

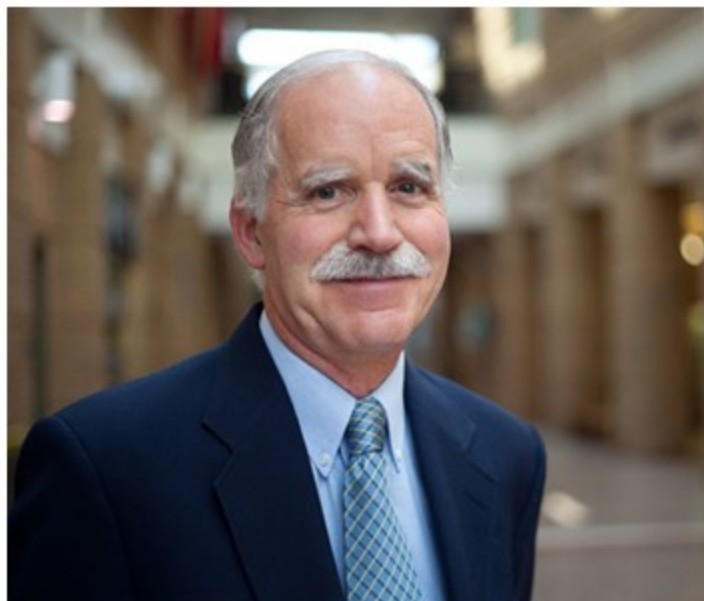


ACIES

Asociación Colombiana de Ingeniería Estructural

Presentación Técnica

“Strut-and-Tie Method for Analysis and Design of Concrete Members”



Dr. James K. Wight

FACI and FASCE, F.E. Richart, Jr.
Collegiate Professor of Civil Engineering
at the University of Michigan.

Development of the Strut-and-Tie Method for use in ACI Building Code

James K. Wight

**F.E. Richart, Jr. Professor of Civil Engineering
University of Michigan**

My introduction to the need for the strut-and-tie method:

Roof member collapse for a Combined Sewer Overflow (CSO) basin in Michigan

Roof consisted of precast double-tee sections with dapped ends designed following the PCI Design Handbook. Approximately 1 meter of soil was placed over top of basin. Collapse occurred as small earth-mover was smoothing soil fill.

Double-Tee with dapped end; roof of CSO Basin



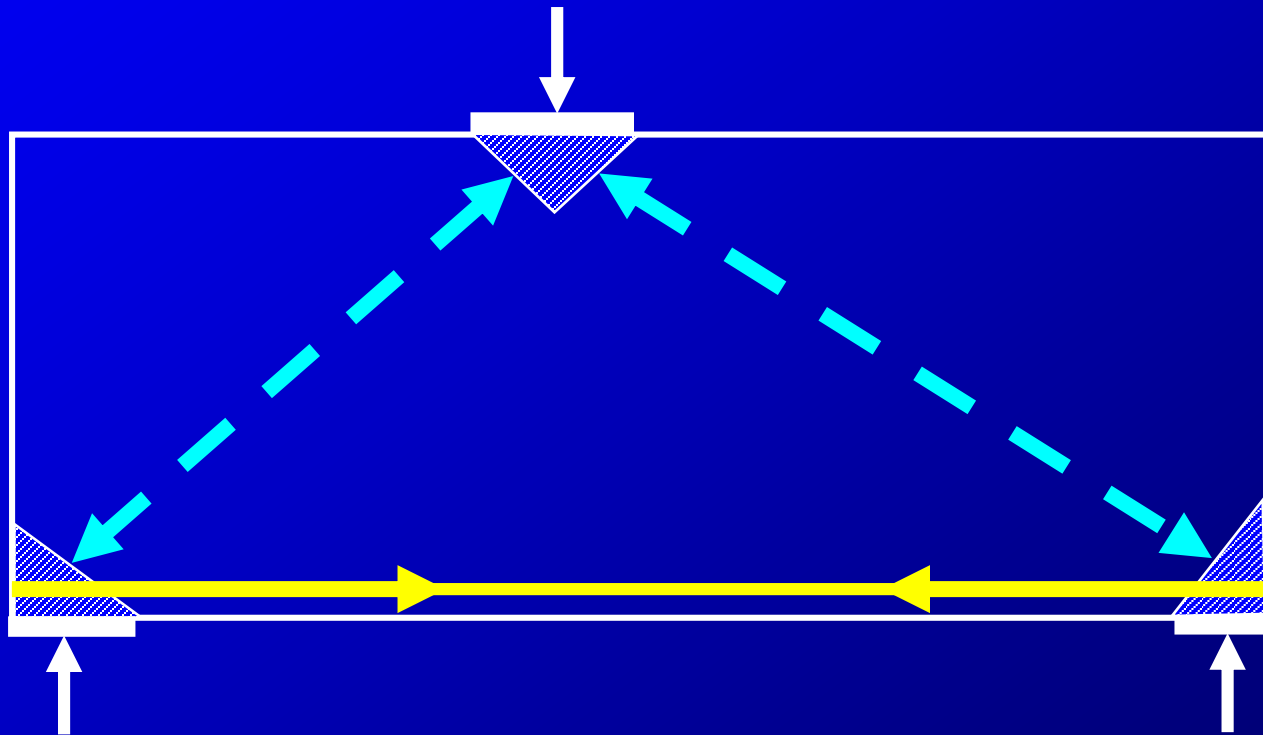
Adjacent uncollapsed roof members



Strut and Tie Models

Members or D-regions (disturbed regions) of members may be designed by idealizing the concrete and reinforcement as an assembly of axially loaded members, connected at nodes, to form a truss capable of carrying loads across a D-region or member.

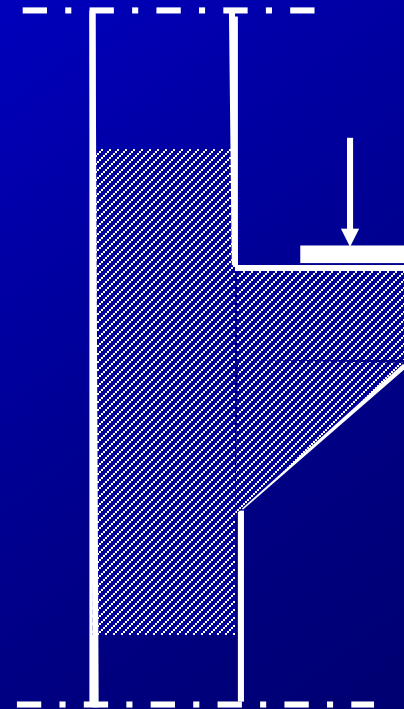
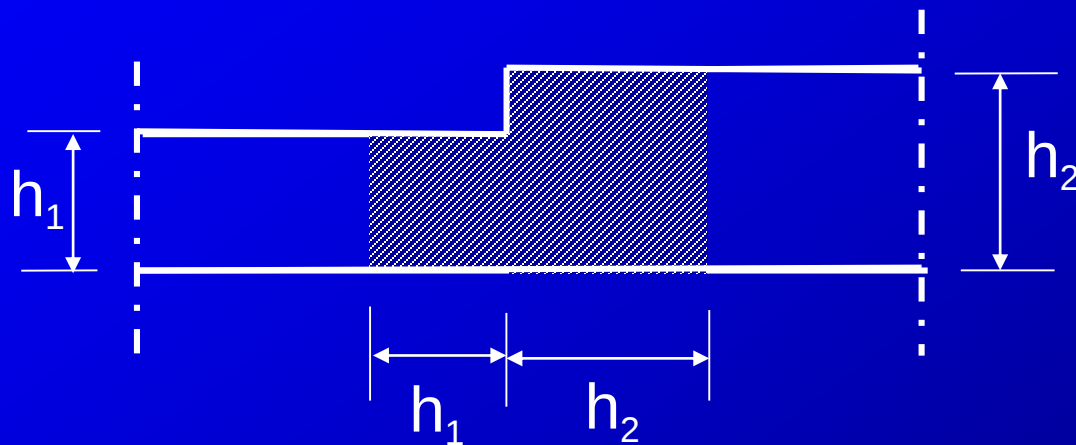
Components of Strut and Tie Models



Steps to Build Strut & Tie Model

- Isolate member or D(disturbed) - region
- Compute forces or distribution of stresses on boundary
- Represent any stress distributions as forces
- Select a truss model to transmit these forces across the member or D-region

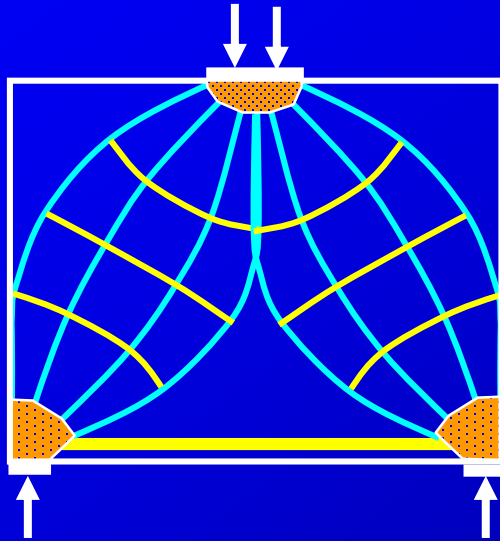
Concept of D-Regions (geometric discontinuities)



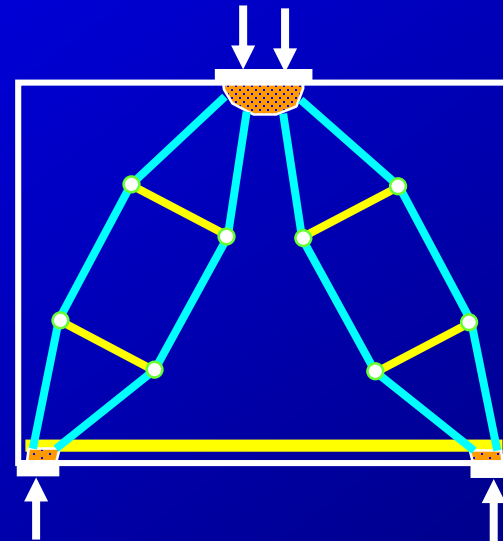
Basic Requirements for STM

- Model approximates stress flow across member or region
- Define truss component dimensions and strengths
- Define ϕ for STM and β factors for struts and nodes
- Analyze struts, ties and nodes
- Select reinforcement; check anchorage

Modeling Stress Flow

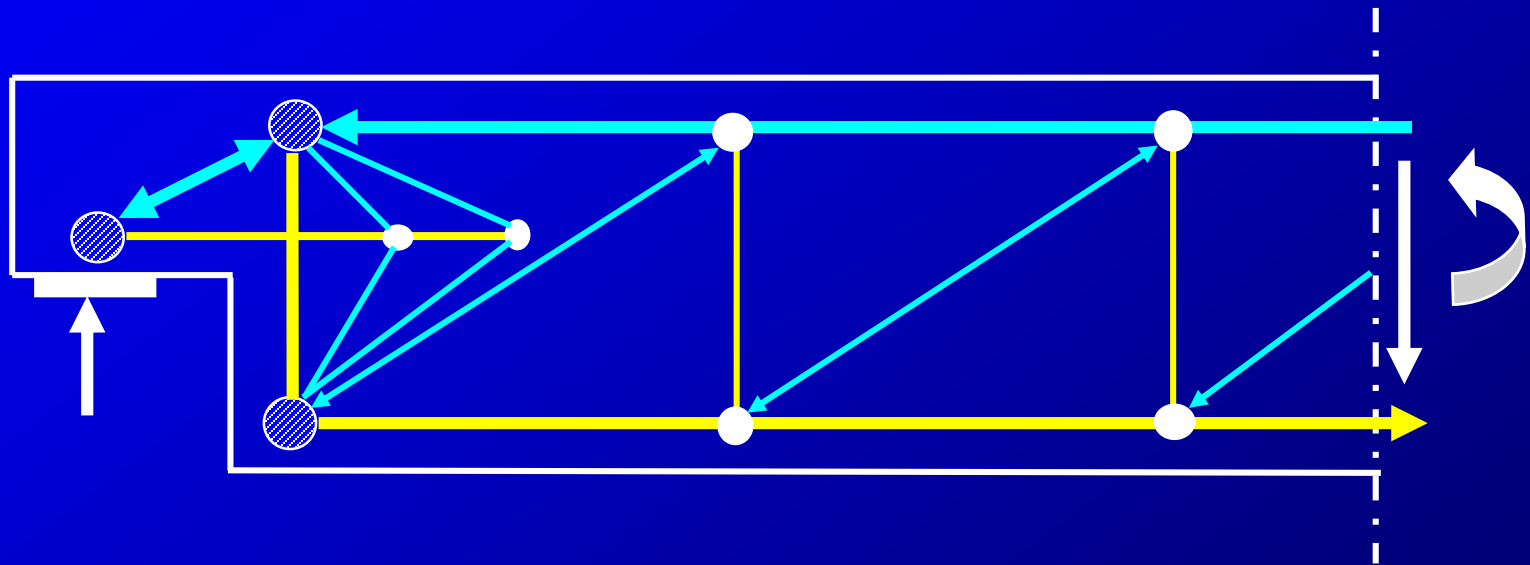


FE Analysis



Truss Model

Modeling Stress Flow in D-Regions (Dapped-End Beam)



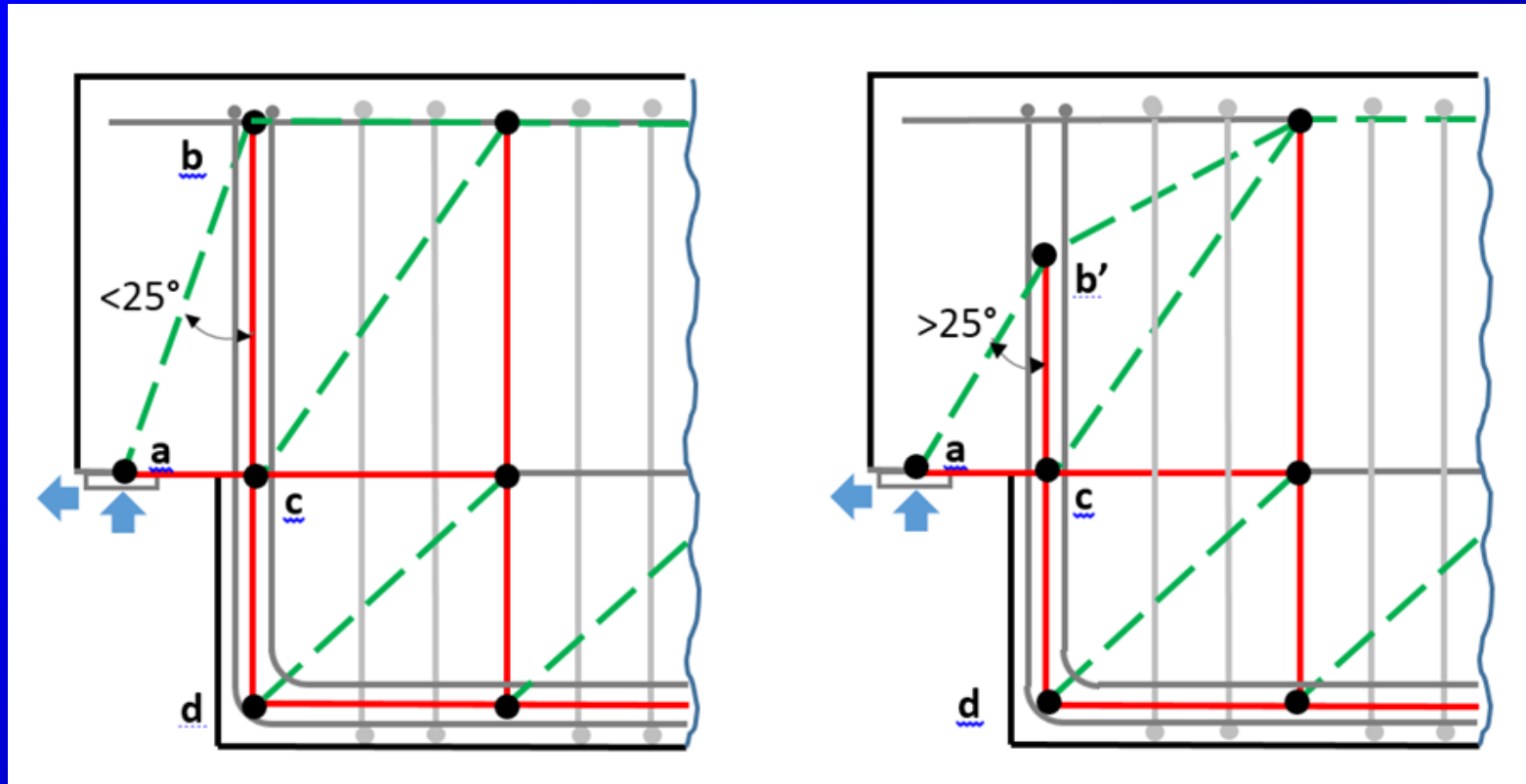
How to Select the “Correct” Strut-and-Tie Model

- Some researchers suggest using a finite element model to determine stress trajectories, then selecting a truss to “model” the stress flow.
- Generally, a STM that minimizes the required amount or reinforcement is close to an ideal model.

Required Definitions for Code

- Geometric rules to follow when creating a strut-and-tie model.
- Component strengths for determining members sizes and final geometry of the model.

Minimum Angle between Struts and Ties



Codes with Rules for Use of Strut-and-Tie Models

- AASHTO LRFD Specification
- Canadian Code for Design of Concrete Structures
- FIP (fib) Recommendations for Design of Structural Concrete

Strength of Compression Struts (what to consider)

- Longitudinal cracking due to transverse tension strain
- Transverse tension forces
- Sustained compression (column design)
- Reinforcement grid crossing strut
- Confinement by concrete or steel

Effective Compressive Strength of Struts

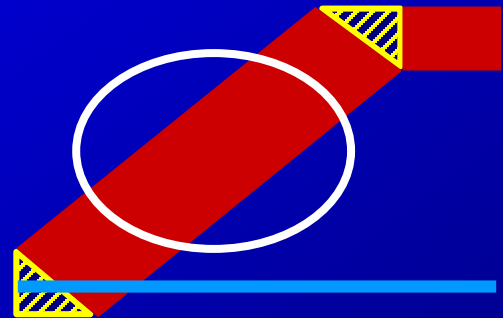
$$\phi F_{ns} \geq F_u$$

$$\phi = 0.75$$

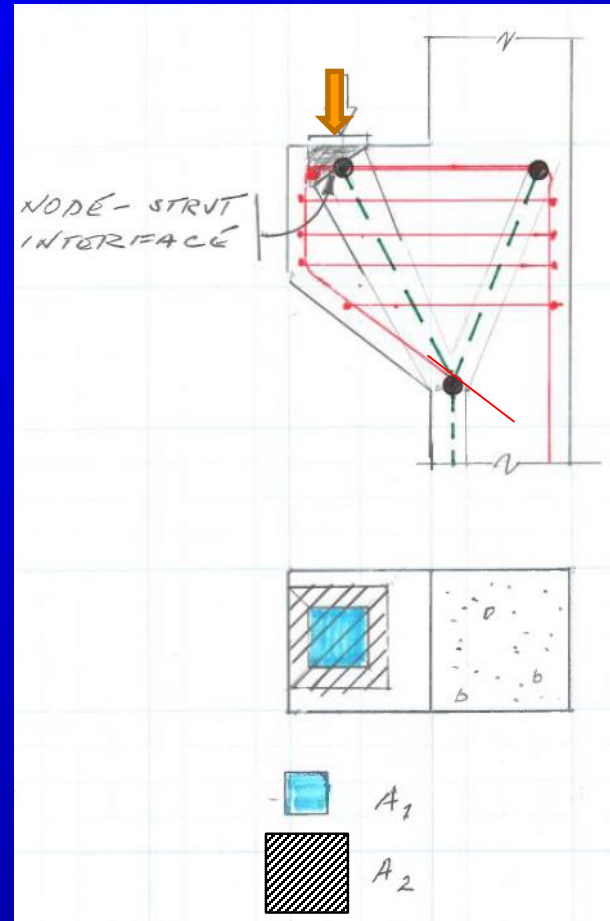
$$F_{ns} = f_{ce} A_c$$

A_c = min. cross - sectional area of strut

$$f_{ce} = 0.85 \beta_c \beta_s f'_c$$



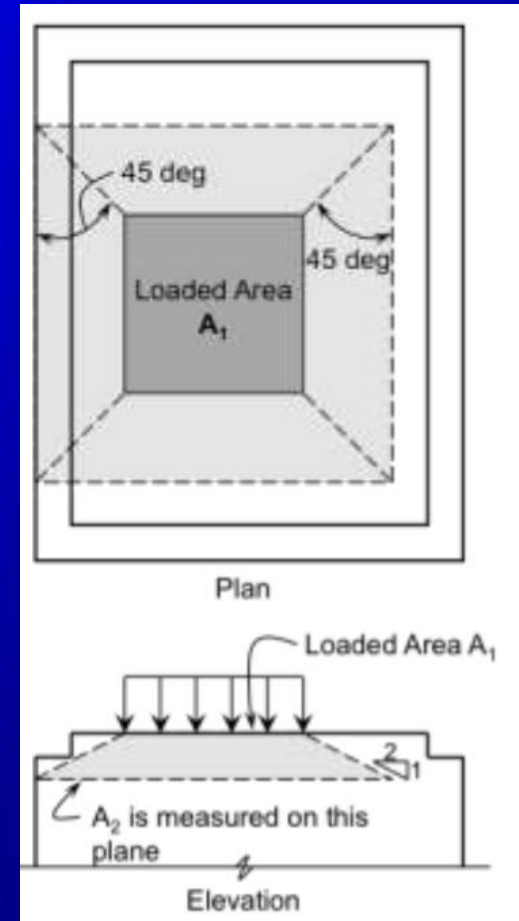
Confined Nodes (and Struts)



Confined Nodes (and Struts)

$$\beta_c = \sqrt{A_2 / A_1} \leq 2.0,$$

otherwise, $\beta_c = 1.0$



CSA Evaluation of Effective Concrete Strength

$$\beta_s f'_c = \frac{f'_c}{0.8 + 170 \varepsilon_1} \leq 0.85 f'_c$$

Transverse tension, $\varepsilon_1 = (\varepsilon_s + 0.002) \cot^2 \theta_s$

θ_s = angle between strut and tie (steel)

ε_s = strain in steel tie

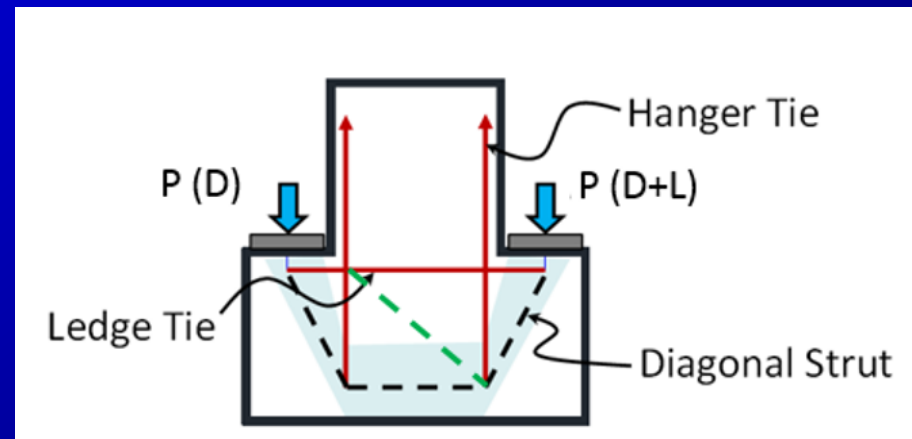
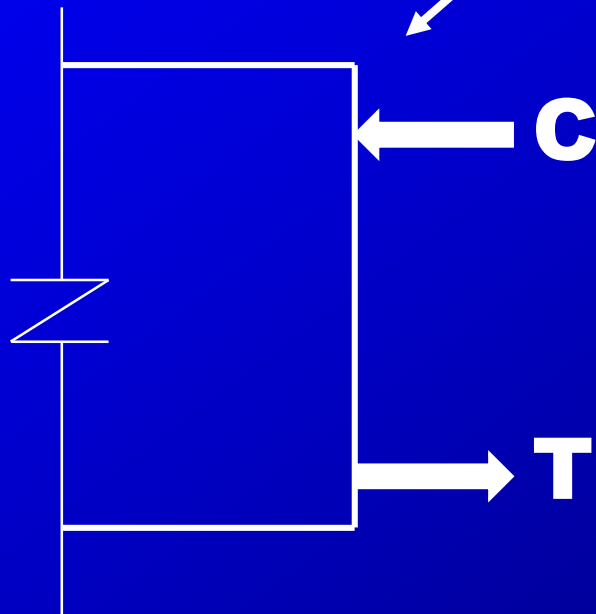
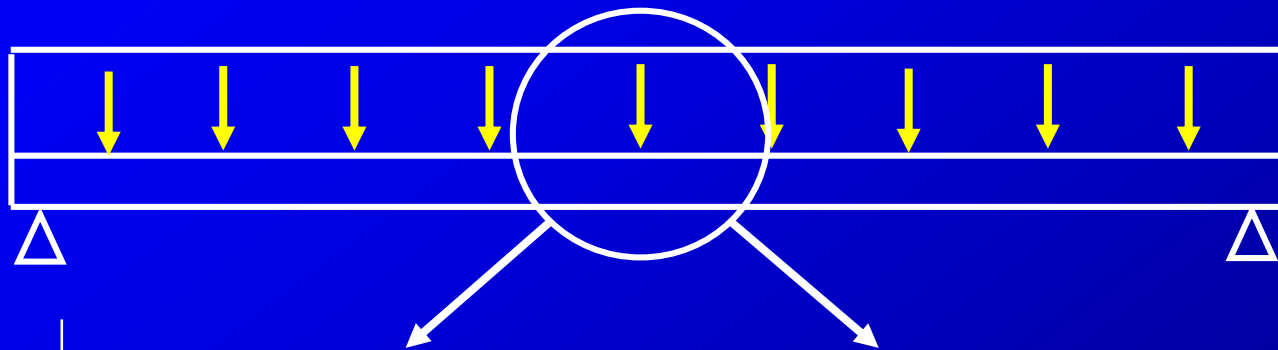
FIP Recommendations for β_s in Cracked Struts

- 0.80 - struts with longitudinal cracking (splitting), but crossed by minimum reinforcement grid
- 0.75 - struts crossed by “normal” width cracks
- 0.60 - struts crossed by “wide” cracks

ACI Recommended β_s Values for Struts

- 1.0 – prismatic shape (constant width) over its length, similar to a flexural compression zone in a B-region
- 0.75 – inclined strut crossed by minimum reinforcement grid
- 0.75 – inclined strut confined by surrounding concrete; for example in a pile cap
- 0.40 – struts in flexural tension zones
- 0.40 – all other cases

Struts in a Flexural Tension Zone



Min. Reinf. Grid in other Codes

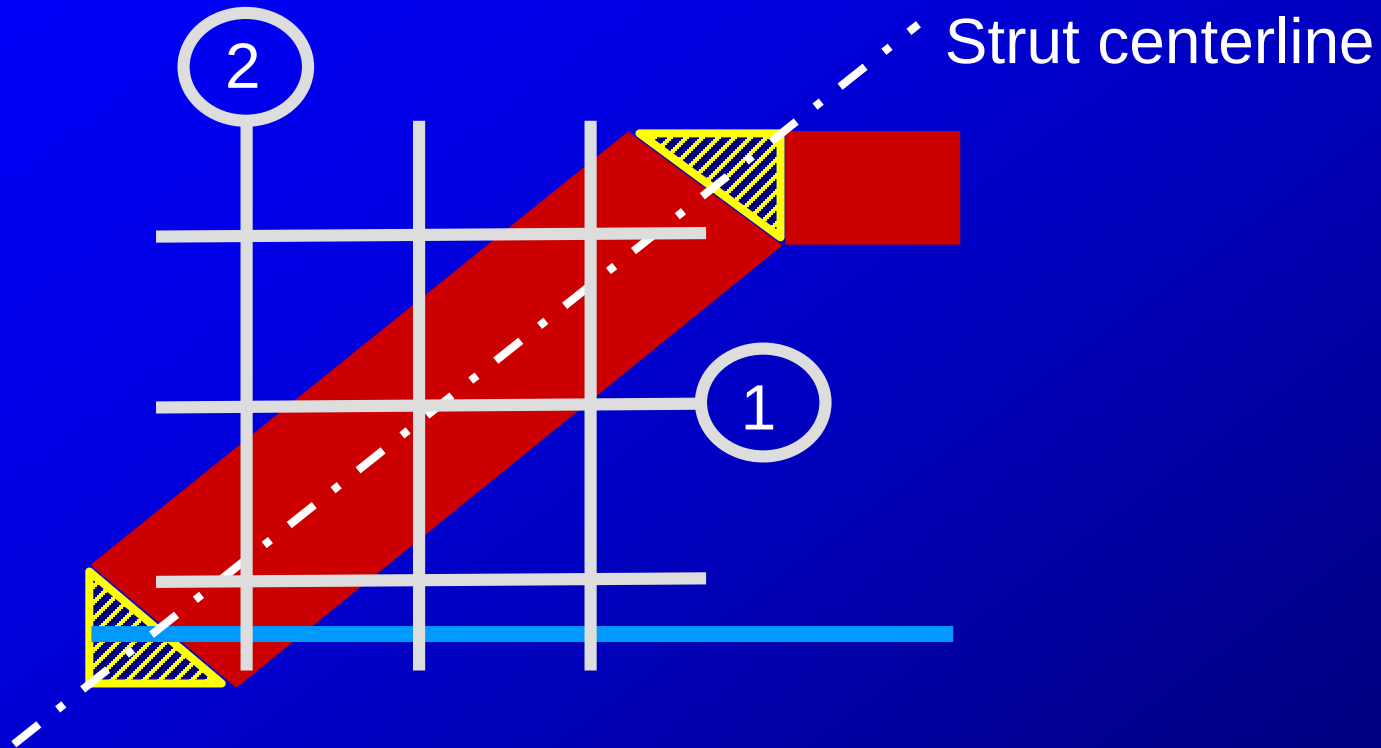
- AASHTO $\rho \geq 0.003 \text{ EW}$
- CSA and FIP $\rho \geq 0.002 \text{ EW}$

Minimum Reinforcement Grid – ACI Code

Deep Beams and Shear Walls with significant shear stresses

$$\rho_\ell \text{ and } \rho_t \geq 0.0025$$

Minimum Reinforcement Grid

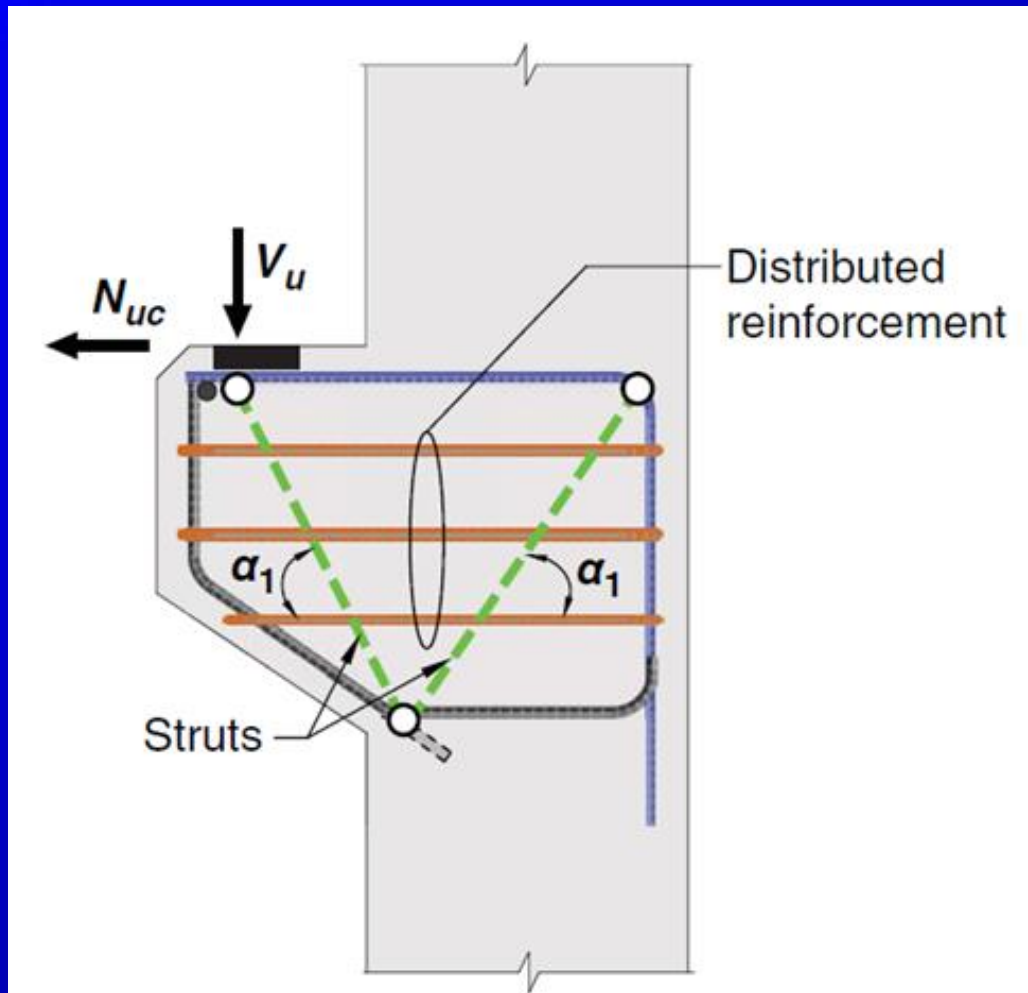


$$\rho_1 \text{ and } \rho_2 \geq 0.0025, \text{ and } s \leq 12 \text{ in.}$$

23.5.1 Minimum Reinforcement Crossing Struts in D-Regions

Reinforcement Configuration	Min. Dist. Reinforcement Ratio
Orthogonal Grid	0.0025 each direction
Reinf. in one direction crossing strut at angle α_1	$\frac{0.0025}{\sin^2 \alpha_1}$

Minimum Reinforcement of D Regions



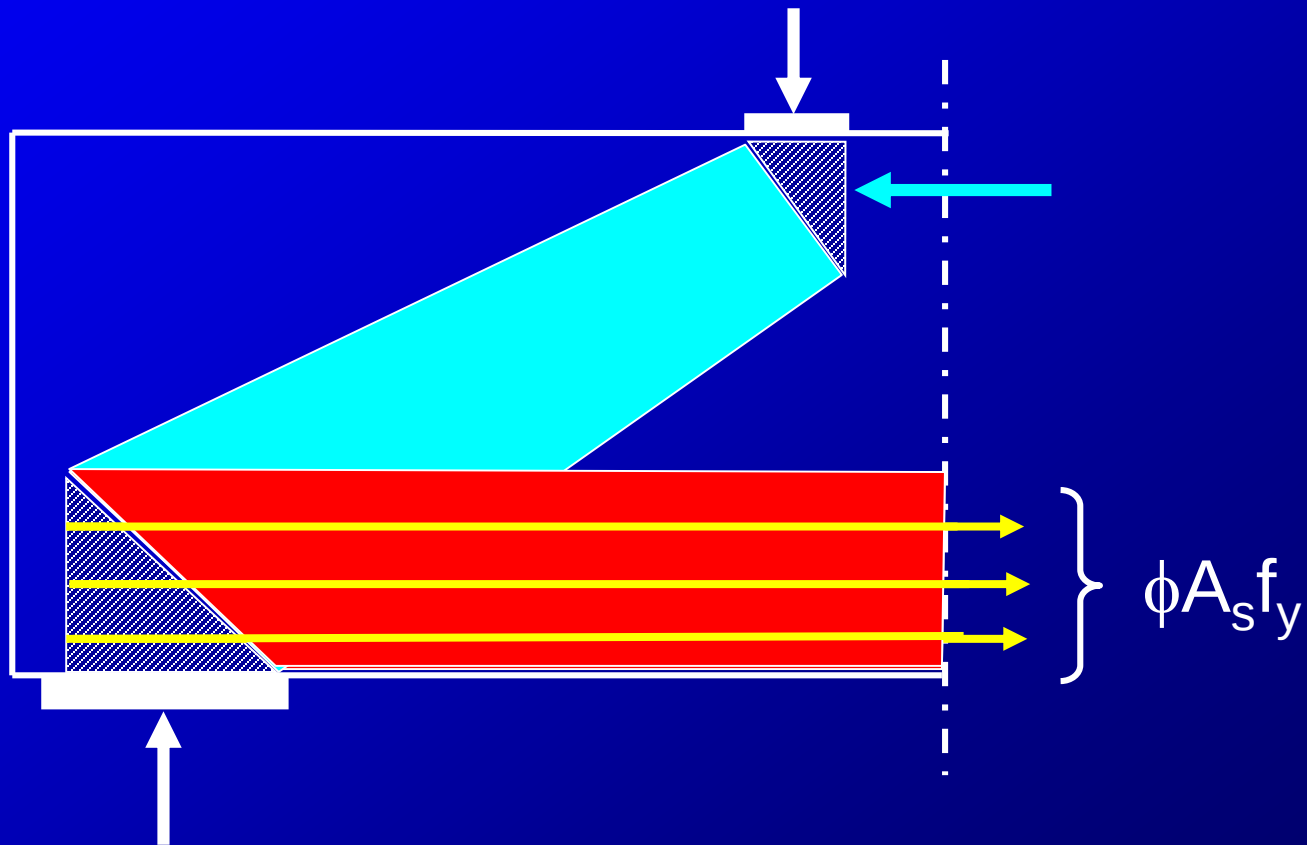
Note: $\alpha_1 > 40^\circ$

**Smaller α_1
governs**

Ties: Dimensions and Strength

- Out of plane - Full width of member
- In-plane width of tie is function of effective compression strength of nodal zone where tie is anchored
- Spread reinforcement throughout tie dimensions

Ties - Dimensions and Strength

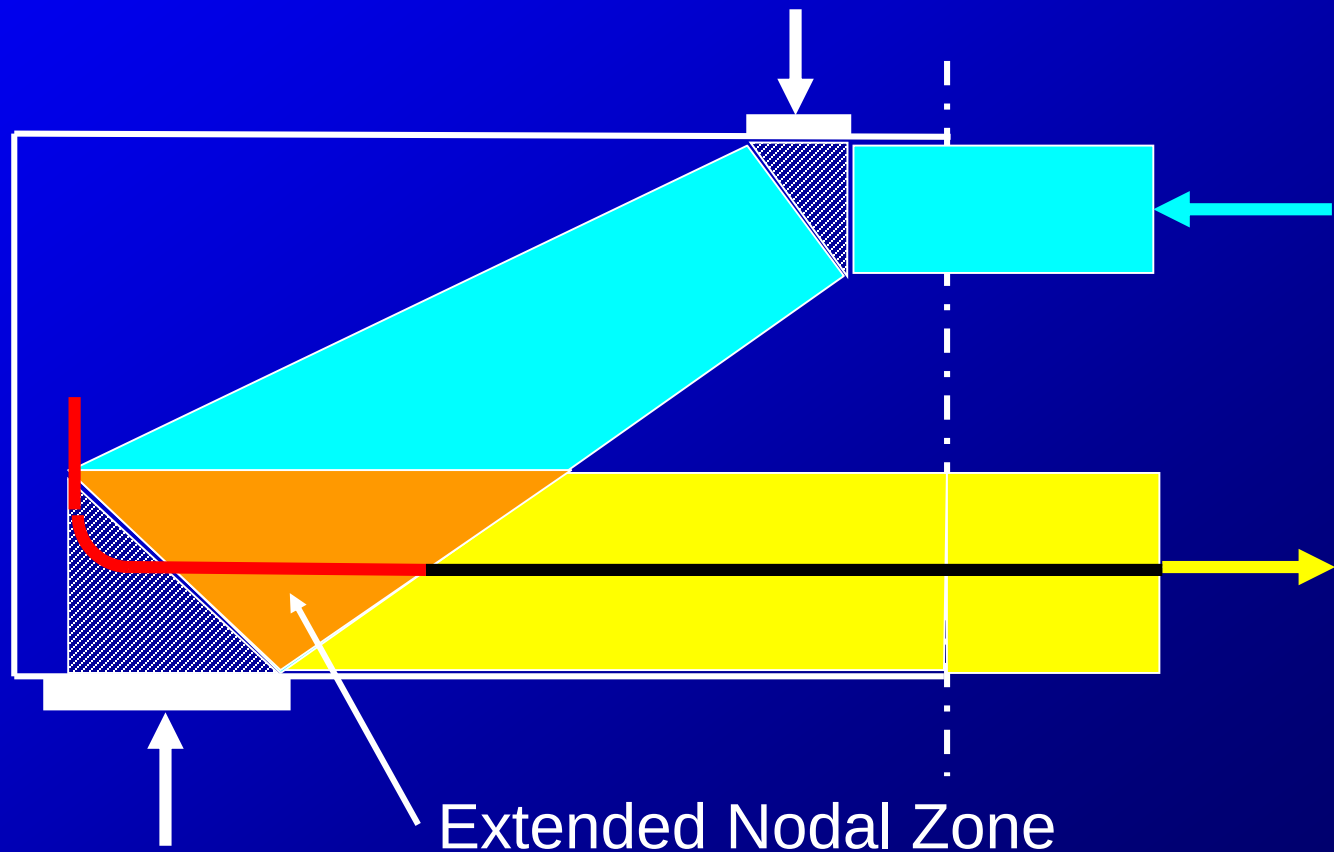


Strength of Ties

- Strength = $\phi A_s f_y$, where $\phi = 0.75^*$
- Anchorage of ties at nodes is a major concern

**A constant value of $\phi = 0.75$ is to be used for sizing the strut-and-tie model.*

Ties - Anchorage Check



Nodal Zones: Dimensions and Strength

- Out of plane - Full width of member
- In-plane: Width of compression face is same as width of strut connecting to nodal zone (smaller allowable strength governs)
- Height of nodal zone is equal to tie force divided by effective compressive strength of the concrete in the node

Effective Strength of Nodal Zones

- Function of type of members connected to the node
- Possible combinations are CCC, CCT and CTT
- Strength can be enhanced by confining concrete or confinement reinforcement

Strength of Nodes

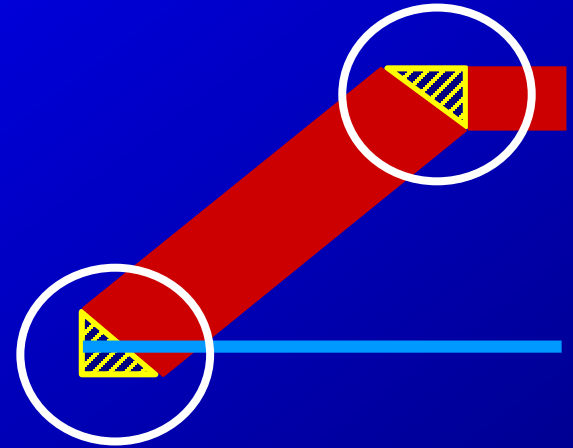
$$\phi F_{nn} \geq F_u$$

$$\phi = 0.75$$

$$F_{nn} = f_{ce} A_n$$

A_n = area of node face $\perp$ to force F_u

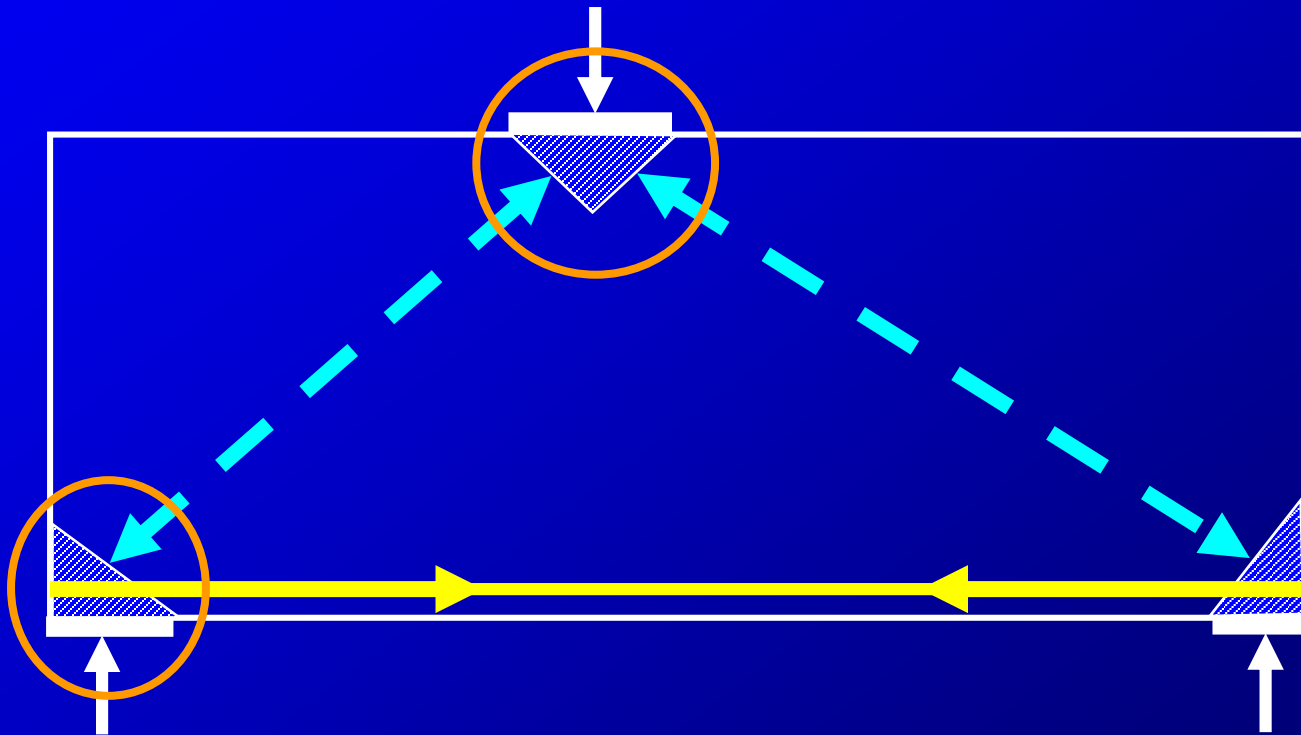
$$f_{ce} = 0.85 \beta_c \beta_n f'_c$$



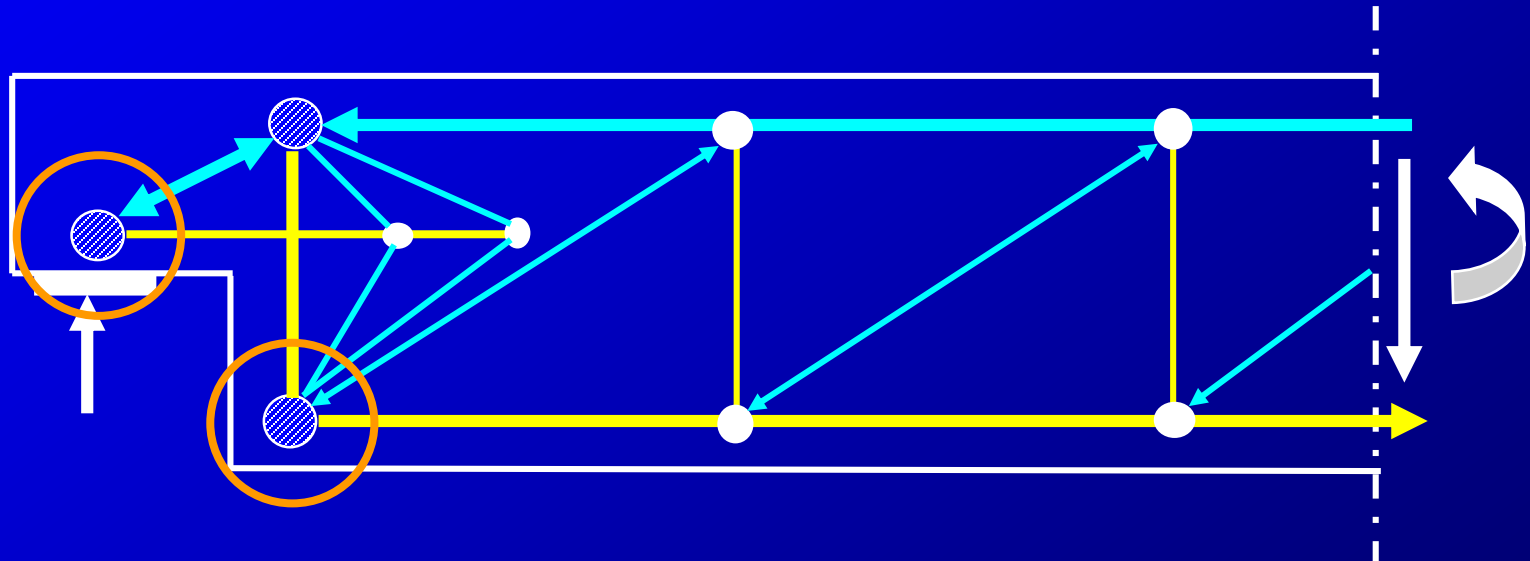
Recommended β_n Values (Nodes)

- 1.0 - CCC node
- 0.8 - CCT node
- 0.6 - CTT node

Examples of CCC and CCT Nodes



Examples of CCT and CTT Nodes



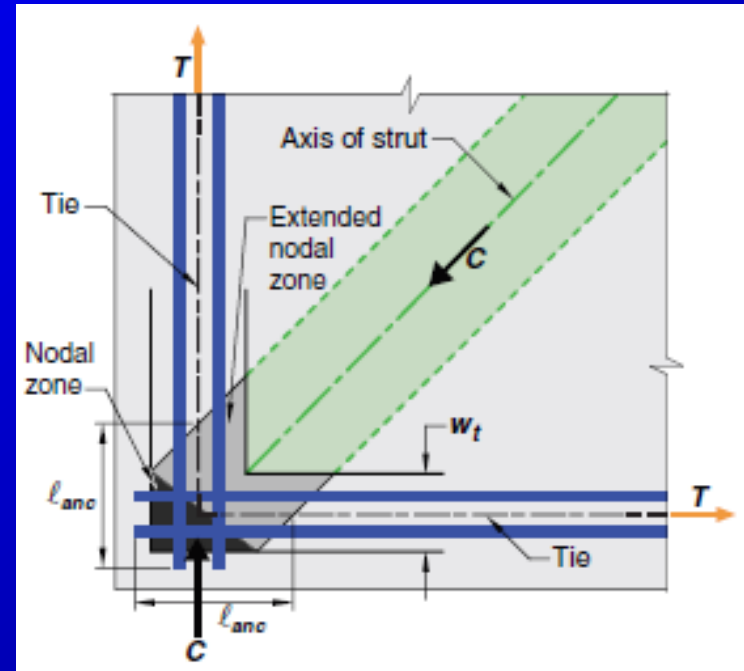
New Items in ACI 318-19

- Curved Bar Nodes
- Use in Earthquake Resistant Design

23.10 Curved-bar Nodes

Why curved-bar nodes?

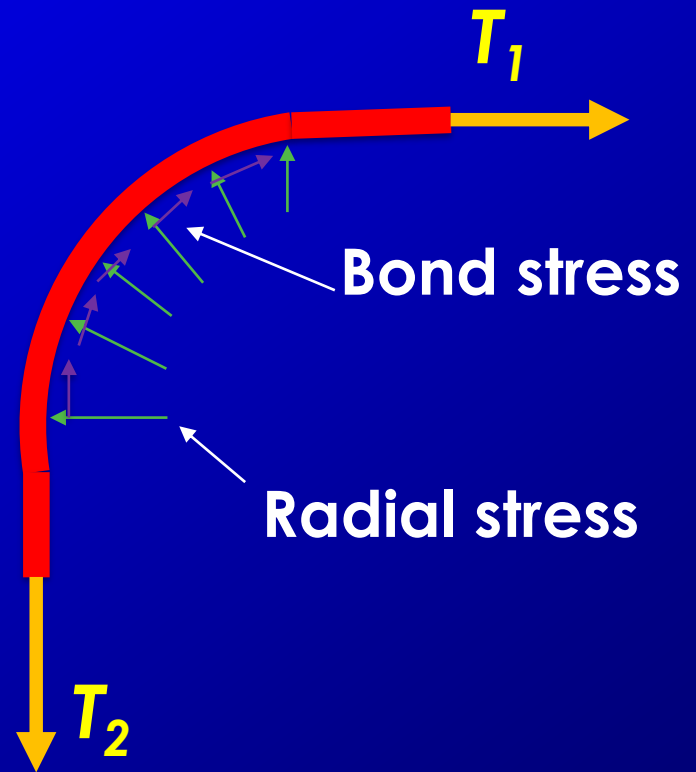
Nodal zones are sometimes too small to allow development



23.10 Curved-bar Nodes

Two issues that need to be addressed:

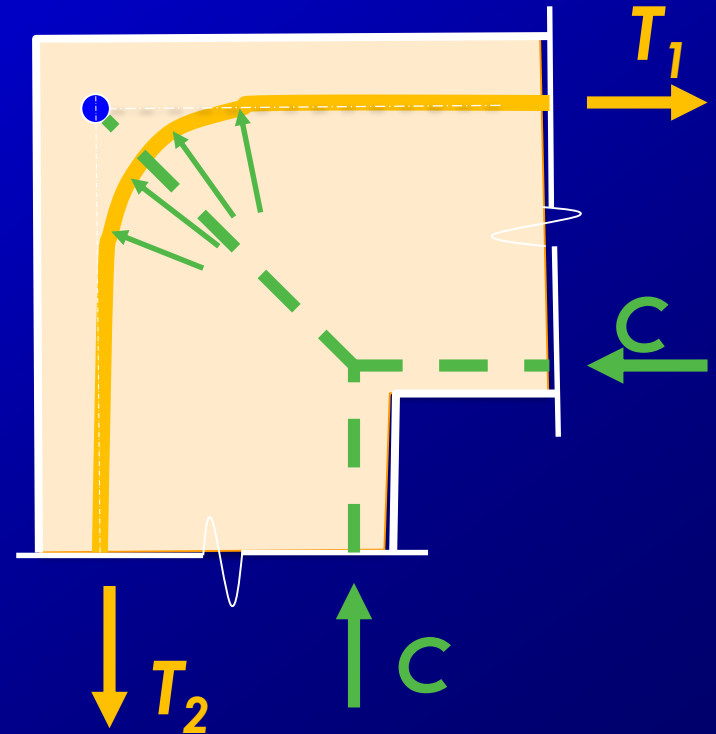
1. Slipping of bar, T_1 and T_2 are not equal.
2. Concrete crushing



23.10 Curved-bar Nodes

1st Condition

- $\theta < 180$ degree bend
- $T_1 = T_2 = A_s f_y$
- Radial compression stresses are uniform
- Bond stresses = 0

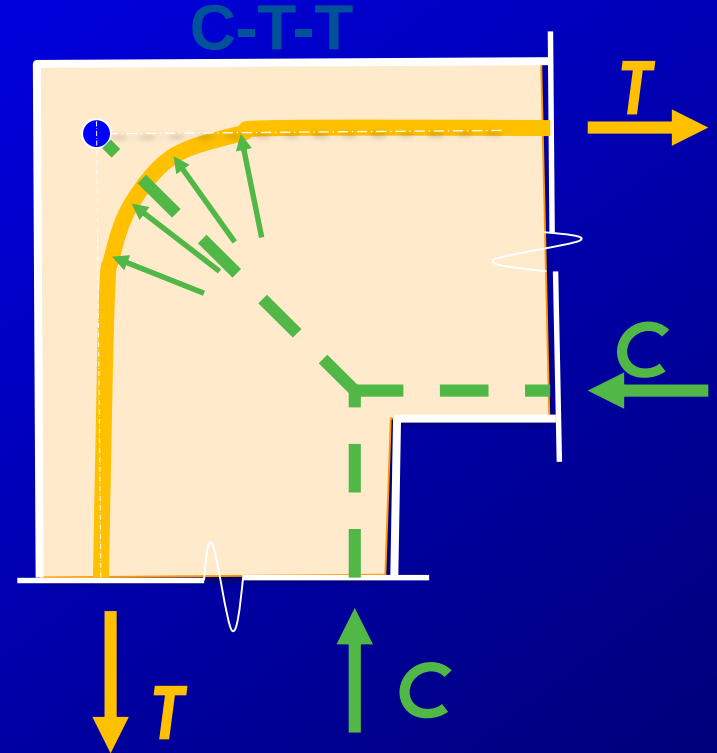


23.10 Curved-bar Nodes

$\theta < 180$ degree bend

$$r_b \geq \frac{2A_{ts}f_y}{bf'_c}$$

but not less than half bend
diameter of Table 25.3;
seldom governs!

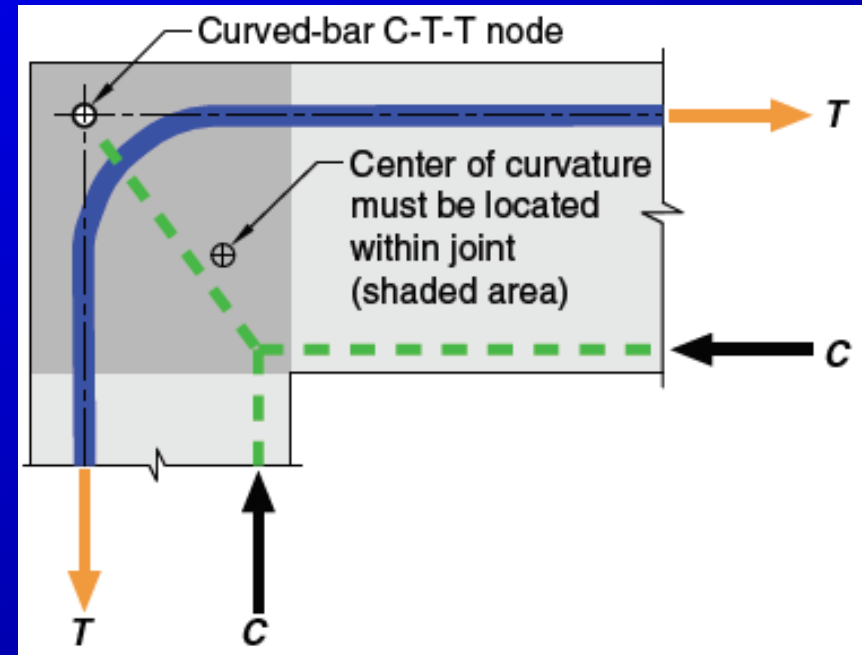


23.10 Curved-bar Nodes

23.10.2 Cover $\geq 2d_b$

23.10.3 Cover $< 2d_b$

$$\rightarrow r_b \times (2d_b / c_c)$$



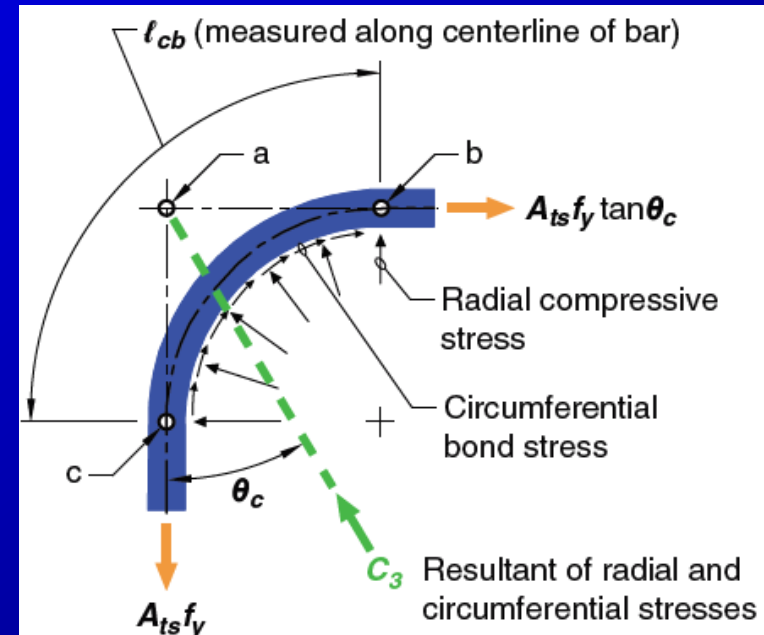
23.10.5 At frame corners, joint and bars must be proportioned such that center of bar curvature is located within the joint

23.10 Curved-bar Nodes

2nd Condition

Tie forces are not equal:

- Compressive stress on the inside radius of bar varies
- Circumferential bond stress develops along bar



$$C_3 = \frac{A_{ts} f_y}{\cos \theta_c}$$

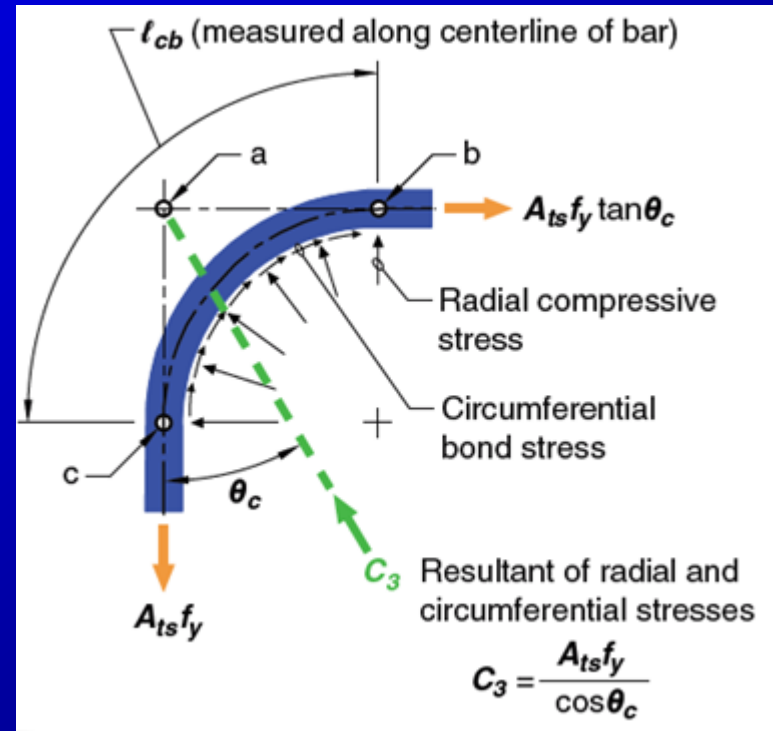
23.10 Curved-bar Nodes

23.10.6 The curve must be sufficient to develop difference in force

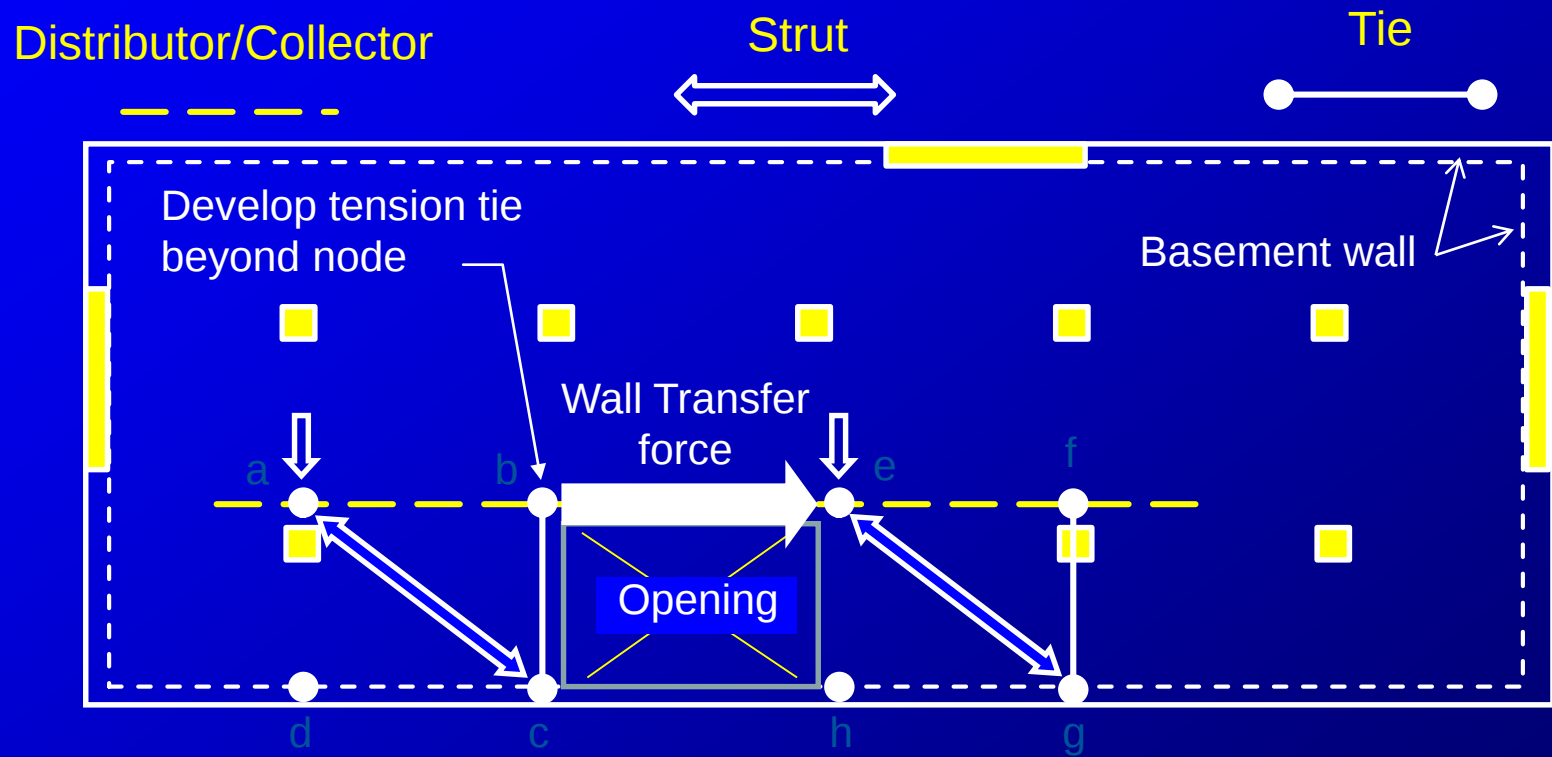
$$\ell_{cb} > \ell_d(1 - \tan \theta_c)$$

In terms of r_b

$$r_b > \frac{2\ell_d(1 - \tan \theta_c)}{\pi} - \frac{d_b}{2}$$



23.11 Earthquake-resistant design using STM



Earthquake-resistant design using STM

Seismic-force-resisting system assigned to SDC

D-F and designed with STM must satisfy:

1. Chapter 18
2. Strut forces are increased by overstrength factor $\Omega_o = 2.5$ or $\Omega_o < 2.5$ if based on rational analysis

23.11 Earthquake-resistant design using STM

If condition 2 is not satisfied then the following must be addressed, Provisions 23.11.2 - 23.11.5

Reduce strut and node effective

compressive strength, f_{ce} , of concrete by 0.8

$$f_{ce} = (0.8)(0.85 \beta_c \beta_{s/n} f_c')$$

Use of STM in ACI 318-19

- Chapter 23 of ACI Code.
- STM is the required procedure for design of deep beams.
- STM is noted as alternate procedure in other sections of the code.
- Sect. 23.11 added for earthquake-resistant design.

Gracias

Questions?

Thank you for your
attention